

WHAT IS CLAIMED IS:

1. A numerical calculation method for a physical quantity U practiced on a computer by solving $A \cdot U = f$, wherein A is a coefficient matrix (in N rows by N columns; wherein N is a positive integer) obtained through discrete of a partial differential equation to be satisfied by said physical quantity U , and f is an inhomogeneous term (source term), comprising the processes of:

setting an initial value U^0 of said physical quantity U ;

setting 0 as an initial value of a number m of repeating times, giving 0 as an initial value of a perturbation quantity ϕ and setting $(f - A \cdot U^0)$ as an initial value r^0 of a residual r ; and

repeatedly executing a first step and a second step while incrementing said number m of repeating times until an approximate solution U^m is converged,

wherein said first step includes the steps of:

obtaining a predicted approximate value ψ^m of $A \cdot \phi = r^m$ through repeated calculation performed by a first calculation unit including an internal solver, and

said second step includes the steps of:

obtaining, from said predicted approximate value ψ^m , a corrected approximate value ϕ^m for minimizing L^2 norm of a residual r^m through an optimization routine performed by a second calculation unit; and

giving $(U^m + \phi^m)$ as an approximate solution U^{m+1} and giving $(r^m - A \cdot \phi^m)$ as a residual r^{m+1} ,

wherein in said second step, obtained elements of a vector sequence $A \cdot \phi^m$ are sampled by a given sampling method to be stored in a memory, and

a residual minimization coefficient α_l^m (wherein $l = 1, \dots, L$) used for obtaining said corrected approximate value ϕ^m is approximately obtained by using elements of a

vector sequence $A \cdot \phi^k$ (wherein $k = m - L + 1, \dots, m - 1$) stored in said memory.

2. The numerical calculation method of Claim 1,

wherein in sampling of elements b_1, b_2, \dots and b_N of said vector sequence $A \cdot \phi^m$ performed in said second step, elements b_i (wherein $i \in \Omega$) are selected, whereas a subset Ω is defined as follows:

$$\Omega = \{i : \text{mod}[i, lg] = 1\} \cup \{i : |f_i/a_{ii}| > \beta\}$$

wherein lg is an integer, β is a real number, f_i is an element of said source term and a_{ii} is a diagonal term on the i th row in the i th column of said matrix A .

3. A numerical calculator for a physical quantity U by solving $A \cdot U = f$, wherein A is a coefficient matrix (in N rows by N columns; wherein N is a positive integer) obtained through discrete of a partial differential equation to be satisfied by said physical quantity U , and f is an inhomogeneous term (source term), performing the processes of:

setting an initial value U^0 of said physical quantity U ;

setting 0 as an initial value of a number m of repeating times, giving 0 as an initial value of a perturbation quantity ϕ and setting $(f - A \cdot U^0)$ as an initial value r^0 of a residual r ; and

repeatedly executing a first step and a second step while incrementing said number m of repeating times until an approximate solution U^m is converged,

wherein said first step includes the steps of:

obtaining a predicted approximate value ψ^m of $A \cdot \phi = r^m$ through repeated calculation performed by a first calculation unit including an internal solver, and

said second step includes the steps of:

obtaining, from said predicted approximate value ψ^m , a corrected approximate value ϕ^m for minimizing L^2 norm of a residual r^m through an optimization routine

performed by a second calculation unit; and

giving $(U^m + \phi^m)$ as an approximate solution U^{m+1} and giving $(r^m - A \cdot \phi^m)$ as a residual r^{m+1} ,

wherein in said second step, obtained elements of a vector sequence $A \cdot \phi^m$ are sampled by a given sampling method to be stored in a memory, and

5 a residual minimization coefficient α_l^m (wherein $l = 1, \dots, L$) used for obtaining said corrected approximate value ϕ^m is approximately obtained by using elements of a vector sequence $A \cdot \phi^k$ (wherein $k = m - L + 1, \dots, m - 1$) stored in said memory.

4. The numerical calculator of Claim 3,

wherein in sampling of elements b_1, b_2, \dots and b_N of said vector sequence $A \cdot \phi^m$
10 performed in said second step, elements b_i (wherein $i \in \Omega$) are selected, whereas a subset Ω is defined as follows:

$$\Omega = \{i : \text{mod}[i, \lg] = 1\} \cup \{i : |f_i/a_{ii}| > \beta\}$$

wherein \lg is an integer, β is a real number, f_i is an element of said source term and a_{ii} is a diagonal term on the i th row in the i th column of said matrix A .

15 5. A recording medium that stores a numerical calculation program for a physical quantity U by allowing a computer to solve $A \cdot U = f$, wherein A is a coefficient matrix (in N rows by N columns; wherein N is a positive integer) obtained through discrete of a partial differential equation to be satisfied by said physical quantity U , and f is an inhomogeneous term (source term),

20 wherein said numerical calculation program makes said computer to execute the processes of:

setting an initial value U^0 of said physical quantity U ;

setting 0 as an initial value of a number m of repeating times, giving 0 as an initial value of a perturbation quantity ϕ and setting $(f - A \cdot U^0)$ as an initial value r^0 of a

25 residual r ; and

repeatedly executing a first step and a second step while incrementing said number m of repeating times until an approximate solution U^m is converged,

wherein said first step includes the steps of:

obtaining a predicted approximate value ψ^m of $A \cdot \phi = r^m$ through repeated

5 calculation performed by a first calculation unit including an internal solver, and

said second step includes the steps of:

obtaining, from said predicted approximate value ψ^m , a corrected approximate value ϕ^m for minimizing L^2 norm of a residual r^m through an optimization routine performed by a second calculation unit; and

10 giving $(U^m + \phi^m)$ as an approximate solution U^{m+1} and giving $(r^m - A \cdot \phi^m)$ as a residual r^{m+1} ,

wherein in said second step, obtained elements of a vector sequence $A \cdot \phi^m$ are sampled by a given sampling method to be stored in a memory, and

a residual minimization coefficient α_l^m (wherein $l = 1, \dots, L$) used for obtaining

15 said corrected approximate value ϕ^m is approximately obtained by using elements of a vector sequence $A \cdot \phi^k$ (wherein $k = m - L + 1, \dots, m - 1$) stored in said memory.

6. The recording medium of Claim 5,

wherein in sampling of elements b_1, b_2, \dots and b_N of said vector sequence $A \cdot \phi^m$ performed in said second step, elements b_i (wherein $i \in \Omega$) are selected, whereas a subset Ω

20 is defined as follows:

$$\Omega = \{i : \text{mod}[i, \lg] = 1\} \cup \{i : |f_i/a_{ii}| > \beta\}$$

wherein \lg is an integer, β is a real number, f_i is an element of said source term and a_{ii} is a diagonal term on the i th row in the i th column of said matrix A .